

2020 Nobel Prize for Physics: Black holes and the Milky Way's darkest secret

Introduction

The Nobel Prize for physics this year was awarded jointly to Roger Penrose, Reinhard Genzel and Andrea Ghez. The prize recognizes theoretical and experimental advances made in the physics and astronomy of black holes. Black holes have long fascinated the lay public as well as scientists. They appear in our language, movies, sitcoms and science fiction. Scientists are obsessed with them as they lie at the edge of our current understanding of the Universe. The scientists honoured by the prize have been instrumental in teasing out the dark secrets of these mysterious objects. There was a time that the very existence of black holes was seriously doubted. With advances in science, technology and understanding, we now realize that black holes are commonplace in the Universe. Every galaxy worth the name has one. Indeed, there's one right in our backyard, in the Milky Way. While their existence is firmly established, black holes continue to throw up challenges to our understanding of the Universe. The physics and astronomy of black holes remain a vibrant field. The prize recognizes the advances which have already been made in this field and provides a stimulus for those which are yet to come.

Roger Penrose (b. 1931) is a theoretical and mathematical physicist at the University of Oxford, UK. He has done seminal work in Einstein's General Theory of Relativity. He has also thought deeply about the foundations of quantum

mechanics and its relation to relativity. His interests include the philosophy of science and its popularization. He also enjoys recreational mathematics and shares his enthusiasm with the lay public. As his drawings on the blackboard and illustrations in his writings reveal, he is also no mean artist.

Reinhard Genzel (b. 1952) is an astrophysicist at the Max Planck Institute for Extraterrestrial Physics, Garching near Munich. He also has affiliations with the Ludwig Maximilian University in Munich and the University of California, Berkeley, USA.

Andrea Ghez (b. 1965) is an astronomer at the University of California, Los Angeles, USA. She has devoted her life to understanding the centre of our Galaxy, the milky way. She is the fourth woman to win the Nobel Prize in Physics.

Half of the Nobel Prize is awarded to Roger Penrose and the other half shared between Reinhard Genzel and Andrea Ghez.

In the rest of this article, we set this year's prize in historical perspective, describe the genesis of the idea of a black hole, the sustained scepticism that delayed wide acceptance of the idea, accumulation of experimental evidence for their reality and some of the challenges that remain for fundamental physics and astronomy.

Prehistory of black holes

The idea of a black hole occurred independently to two polymaths – John

Mitchell and Pierre-Simon Laplace – separated in time by thirteen years and in space by the English channel. John Mitchell was an English clergyman well versed in astronomy, geology, optics and gravitation. He was working within the Newtonian scientific paradigms of his day: the Newtonian theory of gravity, corpuscular light and a geometric interpretation of mechanics. Mitchell (1783) based his reasoning on the idea of escape speed, the speed needed for a projectile to escape to infinity from the surface of an astronomical object. This speed is about 11 km/sec for the Earth and about 600 km/sec for the Sun. These speeds are far less than the speed of light which travels at 300,000 km/sec. However, if there is a body with same density as the Sun and about 500 times its diameter, even light would not be able to escape. Thus, he concluded that the most massive bodies in the Universe may be invisible! We may only be able to deduce their existence by their gravitational influence on other stars. To quote John Mitchell, '... we could have no information from light; If any other luminous bodies would happen to revolve around them we might still perhaps from the motions of these revolving bodies infer the existence of the central ones with some degree of probability.' As we will see below, this is precisely what has been done by the astronomers Genzel and Ghez of this year's prize.

The same idea was independently conceived in France by Pierre-Simon de Laplace in 1796. Laplace, sometimes called the French Newton, worked on topics as diverse as astronomy, probability, surface tension and the origin of the solar system. In his *The System of the world* he stated: 'Therefore there exists, in the immensity of space, opaque bodies as considerable in magnitude and perhaps as equally numerous as the stars'. Laplace's arguments were mathematically more sophisticated than his contemporaries, using differential calculus in contrast to the geometric arguments of John Mitchell. But the content was the same: the Universe may contain 'dark stars'. Or in Laplace's words, 'The largest bodies in the Universe may well be invisible by reason of their magnitude'.



Roger Penrose



Andrea Ghez



Reinhard Genzel

(Figure credit: Roshni Rebecca Samuel)

These prescient speculations lay in obscurity for over a century and were only revived in the 20th Century with Einstein's General Theory of Relativity.

Black holes in general relativity: an idea delayed

In 1915, Einstein proposed his General Theory of Relativity (GTR) which explained gravitation as the curvature of spacetime. In about a month, Karl Schwarzschild discovered the most elementary solution of Einstein's equations, which described the spherically symmetric gravitational field of a point mass M . The solution had the feature that the curvature grew without bound as one approached the centre of symmetry, a feature that mathematicians describe as a 'singularity'. This was not entirely unexpected. The Newtonian gravitational field of a point mass also grows without bound as one approaches the centre of symmetry. However, there was also something intriguing happening at a finite radius $r = 2GM/c^2$, where G is Newton's gravitational constant and c the speed of light. This was not properly understood at the time. Some of the expressions describing the geometry seemed to vanish and others to blow up, evading a clear physical interpretation. There seemed to be some confusion between space and time at this 'Schwarzschild radius'. Researchers named it the Schwarzschild 'Singularity' and moved on. They could afford to do so. In any known astronomical body, the problem did not appear, as the Schwarzschild singularity was deep inside the body, where the vacuum Schwarzschild solution did not apply. For instance, the Schwarzschild radius of the Earth is 1 cm and that of the Sun is 3 km. The problem would only appear if the body collapses gravitationally to within its Schwarzschild radius. This means squeezing the earth to within the size of a marble. Or the Sun to within the size of a small town.

In due course, the problem did appear. Arthur Eddington was a renowned astronomer at Cambridge who worked on the life and death of stars. It was known then that stars shine by burning nuclear fuel in their cores. The heat released in these reactions causes molecular motions and generates pressure which supports the star against its own gravity. Over millions of years the star shines and exhausts its nuclear fuel. It then cools

and in the absence of thermal molecular motions, contracts under its own gravity. A star with the mass of the Sun would contract till it becomes a White dwarf, a star not much bigger than the Earth, which is supported by the quantum mechanical motions of electrons required by the uncertainty principle. Eddington and most of his contemporaries believed that spent stars would find their final repose as white dwarfs.

This peaceful state of affairs was disturbed by a young Indian, a graduate of Presidency College, Madras who was then working in Cambridge: Subrahmanyan Chandrasekhar. Chandrasekhar applied himself to understand the equilibrium of White dwarfs. In 1931, he discovered that as the mass of the star gets bigger, the electrons have to move faster and faster to exert enough pressure to counteract gravity. However, the motion of electrons is limited by the speed of light and if the mass of the star exceeds 1.4 times the solar mass, gravity wins out and the white dwarf is unstable to gravitational collapse. Eddington refused to believe this conclusion. He did not have a scientific argument against Chandrasekhar's reasoning, but only a conviction that 'Nature could not behave in this absurd fashion'! Nevertheless, Eddington's eminence and authority prevailed and the idea of a black hole lay on the shelf for a few more years.

Was there any force that could stop this gravitational collapse? The answer came in the late nineteen thirties. A paper in 1938 in *Zeitschrift für Physik* by B. Datt, Presidency college Calcutta, gave general solutions of Einstein's equations in spherical symmetry. Datt was more interested in the cosmological context, but the paper was noticed by the Russian school around L. D. Landau. Viewed in time reverse, these cosmological solutions can be interpreted as the interior view of gravitational collapse.

Oppenheimer and Snyder (1939) at the University of California, Berkeley found solutions of Einstein's equations that showed that a collapsing star would continue to collapse past its Schwarzschild radius. Oppenheimer and Snyder clearly interpret their equations: 'The star thus tends to close itself off from any communication with a distant observer; only its gravitational field persists.' They had correctly identified the event horizon of a black hole. The conclusion was right but the timing was poor. Shortly afterwards,

World War II broke out. Scientific research projects were shelved in favour of the urgent demands of the war effort. Many scientists were involved in the war effort, some of them developing radar to detect enemy planes. Oppenheimer dropped his research on gravitational collapse and went on to lead the Manhattan project. Another delay!

Even in 1939, Einstein was unconvinced by the physical reality of the Schwarzschild radius. Writing in the *Annals of Mathematics* in 1939, he argued that time would stand still at the Schwarzschild radius, a patently absurd conclusion. Also bodies falling into the Schwarzschild radius would appear to hover at the Schwarzschild radius, frozen in time for ever. He seriously doubted that these predictions of his theory had any physical validity. He believed that these absurdities were artefacts of the idealization involved in a point mass. After the famous point mass solution, Schwarzschild had in fact discovered an interior spherically symmetric solution of Einstein's equations. But as Schwarzschild had assumed an incompressible fluid interior, Einstein was able to dismiss this too as an artefact of unreasonable assumptions: in an incompressible fluid, sound would propagate instantaneously, violating relativity.

The high degree of symmetry of the Oppenheimer-Snyder collapsing solution was also a matter of concern. Perhaps the collapse and resultant singularity was a consequence of the artificial initial conditions. Perhaps deviations from spherical symmetry would prevent gravitational collapse. Maybe the matter would 'bounce back' due to other interactions, or release its energy in a burst of gravitational radiation. Many cosmological solutions of Einstein's equations were known. Most of these had singularities either in the past or in the future. Naturally, all the solutions found analytically had a high degree of symmetry, since Einstein's equations are hard to solve without the simplifying assumption of symmetry. The question remained: are total gravitational collapse and singularities generic in General Relativity?

Radio astronomy and relativistic astrophysics

After the war, the world was beating its swords into ploughshares. Radio

engineers turned their war-time instruments to the skies and discovered a whole new window to the Universe. Unlike light, radio waves are not absorbed by dust in the Galaxy and radio telescopes were able to 'see' clear and deep into the cosmic distance. Radio waves were detected from the Milky Way and from other galaxies. A new branch of astronomy was born. As the observations mounted, radio astronomers realized that the skies were not as placid as they appeared. Radio waves were emanating from very tiny regions in the sky. The size of the emitting region had to be less than a light day since the intensity sometimes changed in a few hours. But the spectral lines of these sources showed that they had to be at an enormous cosmic distance. From the energy received at the telescopes, it was clear that some of these point like 'stars' were shining brighter than whole galaxies. They were called quasars or quasi-stellar objects (QSOs) or Active Galactic Nuclei (AGN). Many sources had radio jets, matter ejected at relativistic speeds from the centre (Figure 1). There were violent and energetic events taking place at the centres of galaxies. Tremendous amounts of energy were being released from an object not much larger than our solar system.

What was the source of this energy? Nuclear energy was an unlikely candidate. Nuclear reactions have about a one per cent efficiency in converting mass into energy ($E = mc^2$). It would need enormous amounts of matter to be concentrated into a tiny volume in order to explain the observed energy output. Such concentrations of matter would actually signal a situation close to gravitational

collapse. In such compact objects, the gravitational energy of falling matter could be converted into radiation with an efficiency as high as five per cent (for a non rotating black hole). As more data came in, it was clear that many galaxies had compact objects in their cores. Relativistic astrophysics was born. The Texas symposium in 1963 marked a coming together of mathematics, physics and astronomical observations.

Relativity after Einstein

The period after Einstein's death in 1955 marked a new phase in the development of general relativity. This was the beginning of mathematical relativity. Much of the earlier confusion with 'Singularities' stemmed from the fact that researchers were not sufficiently sophisticated mathematically. They had an undue faith in the coordinates they used to describe space and time. Some 'singularities' are only apparent; they are failures of the coordinate system not features of the spacetime. This is best explained by using geography. Over the Earth, we use latitudes and longitudes to pinpoint locations. However, this method fails at the poles of the Earth, as the longitude is ill defined. But there is nothing special about the poles. This is a removable singularity, a failure of the coordinate system rather than an intrinsic feature of the Earth. What was needed was an appreciation of global methods, which mathematicians had developed for their own purposes. By patching together local descriptions using coordinates, they were able to arrive at a global notion: that of a manifold. With increased sophistication,

it becomes clear that the Schwarzschild 'singularity' is only apparent. There *is* something funny happening at the Schwarzschild radius, but it is not a singularity. It is the event horizon of a black hole!

In the years 1953–1955, Amal Kumar Raychaudhuri, working in Calcutta, studied the motion of a cloud of dust in general relativity and derived an equation (the Raychaudhuri equation) which was to prove central in further developments. The equation expresses the attractive nature of gravity: that neighbouring particle trajectories would tend to focus. Slightly later, a version of the Raychaudhuri equation was independently derived by L. D. Landau in the Soviet Union. Two of his colleagues, E. M. Lifshitz and I. M. Khalatnikov studied the question of whether singularities were generic in general relativity. Their conclusion was negative: singularities were artefacts of symmetry and did not appear generically in the theory.

Roger Penrose was very sceptical of this conclusion. In seminal papers, he applied the Raychaudhuri equation, using some global mathematical techniques from differential topology and geometry to arrive at the opposite conclusion: generic solutions of Einstein's equations contain singularities either in the past (like the big bang) or in the future (as in the centre of a black hole). One of the key ideas he introduced was the global notion of a trapped surface. Imagine a sphere in ordinary space emitting a flash of light. One part of the wave emanating from the sphere moves into the sphere contracts everywhere and decreases in area. The other wave moves out, expands everywhere, increasing in area. In some gravitational fields, like that inside the Schwarzschild radius, it can happen that both these waves (or wave fronts more precisely) are contracting everywhere. This is what Penrose calls a trapped surface. Once a trapped surface forms, Penrose showed that collapse and singularities are inevitable. Small perturbations of the trapped surface in the Schwarzschild spacetime do not destroy the trapped surface and it follows that singularities are generic. More precisely, what he showed was that the spacetime was incomplete. In such a spacetime, photon trajectories would abruptly terminate, suggesting that points of spacetime have been artificially removed from consideration. Putting them back reveals



Figure 1. An artist's impression of a black hole surrounded by an accretion disc emitting a radio jet. Figure credit: Roshni Rebecca Samuel.

the singularity. One of the key assumptions in the theorem was that matter was ‘reasonable’, i.e. there was no negative mass, which is the case with all known forms of matter. Subsequent work by Penrose and Hawking nailed it even more firmly: most spacetimes have singularities.

A blackhole in our backyard

The Nobel prize was awarded for work by two independent groups, who studied the central region of our Galaxy over a period of twenty years and adduced strong evidence for the existence of a black hole in the centre of our Galaxy. The estimated mass of the black hole is 4.0 million times the mass of the Sun and corresponds to a Schwarzschild radius of 10^7 km (40 light seconds). The evidence is based on the observations of the motion of stars in a small region near the centre of the Milky Way. The observations tell us that the stars are in orbit around a massive central object. The motion is consistent with Kepler’s laws of planetary motion. The centre of the Galaxy is 24,000 light years away from us. At this distance, the motion of stars appears as a very tiny angular change in the position of the star in the sky. Astronomers refer to this as ‘proper motion’. Detecting the proper motion is a challenging task. First one needs to build up a celestial reference frame against which proper motions can be measured and followed over decades. One also needs fine angular resolution to distinguish objects in the field of view. In analogy one needs to be able to distinguish between the left and right eye of a man standing 250 km away. The angular resolution of a telescope increases with its size and with its operating frequency. (The best angular resolution one can get with a telescope of size D operating at a wavelength λ is (λ/D) in radians.) Even with large telescopes operating at small wavelengths, there is a problem because the turbulence in the earth’s atmosphere blurs and distorts the image.

The two groups (one led by Genzel and the other by Ghez), studied the region around the source Sagittarius A* near the centre of our Galaxy. This region has fast moving stars and hot ionized gas. The region of interest subtends an angle of only $6''$ (six arc seconds; one arc second is $1/3600$ of a

degree). The theoretical limit on the angular resolution of a telescope of diameter 10 m operating at the infrared wavelength of $2.2 \mu\text{m}$ is a twentieth of an arc second. This is called the diffraction limit. The diffraction limit is hard to achieve because of the turbulent atmosphere, which causes the image to shift on time scales of the order of a second. To beat this problem, the observers used advanced techniques made possible by modern technology. Charge coupled devices (CCD) enabled larger detector efficiency than the older photographic plates, permitting shorter exposures. The observations were made with short expo-

sures (about a tenth of a second). Over this timescale, the atmosphere can be regarded as frozen. The snapshots can then be subject to speckle imaging. In the most basic version, the successive images are combined with a compensatory shift. A more advanced version called speckle interferometry uses Fourier analysis to produce a high resolution image. Another technique used in imaging is adaptive optics. This method measures the atmospheric fluctuations in real time and corrects for the distortion of the image. The atmospheric fluctuations have the effect of corrugating the plane wavefront received from the astronomical

Stars closest to the centre of the Milky Way

The stars’ orbits are the most convincing evidence yet that a supermassive black hole is hiding in Sagittarius A*. This black hole is estimated to weigh about 4 million solar masses, squeezed into a region no bigger than our solar system.

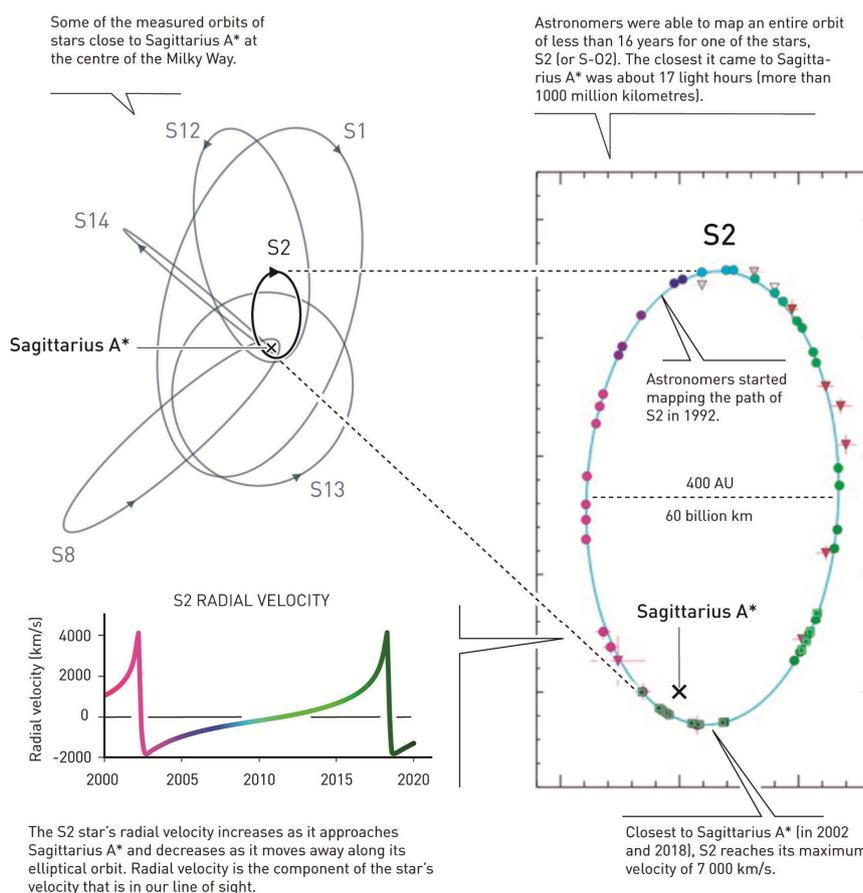


Figure 2. The elliptical orbits of stars around the central object. This figure is the result of decades of observations of stellar motions in the centre of our Galaxy. Remember that the figure shows the projection of orbits in the plane of the sky. In projection the focus of the elliptical (or circular) orbit may not lie at the location of the central object. Figure courtesy: © Johan Jarnestad/The Royal Swedish Academy of Sciences.

source. These corrugations are compensated by having a deformable mirror adapting to cancel the distortion. Early efforts used a 'guide star': a reference star whose apparent position reveals the fluctuations of the atmosphere. A more advanced version uses a laser to create an artificial guide star in the sky which is used as a reference.

By patient observations lasting over decades, the astronomers were able to identify stars orbiting around a central massive object. They were able to observe the motion of the stars in their orbit and even complete orbits. Some of the orbits are extremely elliptical and in the closest approach to the central object give us a weak upper bound on its size. One of the stars has a period of just fifteen years, well within the patience and lifetimes of astronomers.

The stars can be adequately described by Newtonian gravity. Kepler's laws tell us that in the solar system, planets move in elliptical orbits. What the observers see (Figure 2) at the centre of our Galaxy is exactly the same, except that it is scaled up in size. The Sun is replaced by the central black hole, which is 4 million times the mass of the Sun. The planets are replaced by stars traversing elliptical orbits. Tracing the orbits of the stars, measuring their positions and velocities tell us the mass of the central object as well as an upper bound on its

size. Nothing fits the bill like a black hole.

Conclusion

This year's Nobel prize clearly brings out the interaction between theory and experiment in this area of physics. The speculations of Mitchell and Laplace and their illustrious successors were all purely theoretical. It was only with the coming of Radio astronomy in the 1950s that experimental evidence began to emerge. The radio observations of active galactic nuclei showed that many galaxies have black holes in their centres. The question naturally arose: does the Milky Way harbour a black hole, we have measured its mass! The day is not far off when we will also know its spin! The experiments now throw up new challenges for the theory of galactic evolution. Black holes are believed to be important in the evolution of galaxies. The observations reveal that there are a surprising number of young stars in the vicinity of the black hole. One would not have expected this, as black holes tend to tidally disrupt large objects like the gas clouds which form young stars.

The singularity theorems are important developments in Relativity in its modern phase. Apart from telling us clearly that

general relativity predicts black holes, they also tell us that general relativity will fail at some point. A new theory will be needed to understand the singularity. Understanding black holes has also given us hints about the new direction. The irreversible nature of gravitational collapse is reminiscent of other irreversible phenomena in physics like the increase of entropy and the loss of information. Work by Hawking in the 1970s revealed that black holes are thermal objects in quantum physics. It seems very likely that the missing piece of this puzzle is a quantum theory of gravity. This is the holy grail of theoretical physics.

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